Plasmonics with two-dimensional conductors

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A wealth of effort in photonics has been dedicated to the study and engineering of surface plasmonic waves in the skin of three-dimensional bulk metals, owing largely to their trait of subwavelength confinement. Plasmonic waves in two-dimensional conductors, such as semiconductor heterojunction and graphene, contrast the surface plasmonic waves on bulk metals, as the former emerge at gigahertz to terahertz and infrared frequencies well below the photonics regime and can exhibit far stronger subwavelength confinement. This review elucidates the machinery behind the unique behaviours of the two-dimensional plasmonic waves and discusses how they can be engineered to create ultra-subwavelength plasmonic circuits and metamaterials for infrared and gigahertz to terahertz integrated electronics.

1. Introduction

Surface plasmons propagating in the skin of a bulk—three-dimensional—metal with a finite penetration depth have generated a great deal of research in photonics, because they can travel up to approximately 10 times slower than the free-space light (speed c), and thus can exhibit subwavelength confinement with proportionally reduced wavelength [1–4]. In contrast to these surface plasmons on bulk metals that emerge in the optical frequencies, the plasmons in GaAs/AlGaAs two-dimensional electron gas (2DEG) and graphene, where electrons are perfectly confined into two dimensions, appear at infrared and terahertz to gigahertz frequencies, near or in the electronics regime. Furthermore, the two-dimensional plasmons can achieve much greater subwavelength confinement [5–7] with their velocity being able to reach well below c/100 [6,8].
By shaping the two-dimensional conductor geometry with the standard fabrication technology and manipulating two-dimensional plasmonic waves via reflection, interference and coupling according to the geometry, a variety of ultra-subwavelength two-dimensional plasmonic circuits and metamaterials, such as bandgap crystals, interferometers, resonant cavities and negative refractive index structures, can be created [6,8,9] for gigahertz to terahertz and infrared integrated electronics with applications in imaging, large molecule spectroscopy and submillimetre wave astronomy. The ultra-subwavelength confinement of these two-dimensional plasmonic structures suggests exciting possibilities for sub-diffraction-limit imaging, near-field operation and drastic miniaturization.

This review first elucidates the unique behavioural characteristics of plasmonic waves in two-dimensional conducting media and their physical origin (§2). Then we delineate how two-dimensional plasmonic waves can be engineered to build functional circuits and metamaterials using some recent device advances as examples (§3).

2. Physical characteristics of two-dimensional plasmonic waves

Perturbation of the equilibrium electron density distribution in a solid-state conductor—whether three- or two-dimensional—results in Coulomb restoring force, which drives local electrons back and forth collectively to propel a plasmonic wave. The defining energetic component of a plasmonic wave is the kinetic energy of the collectively oscillating electrons, which largely accounts for the plasmons’ behavioural difference from light waves, in particular the reduced plasmonic velocity and subwavelength confinement. The kinetic energy is far more strongly pronounced in two-dimensional plasmonic waves than in three-dimensional bulk metal surface plasmonic waves [6,9]. Consequently, the behaviour of two-dimensional plasmons diverges even more significantly from light waves than three-dimensional surface plasmons; for example, and notably, two-dimensional plasmons can achieve a significantly lower velocity thus a much greater subwavelength confinement than three-dimensional surface plasmons. This section explicates the origin of the unique behaviours of two-dimensional plasmonic waves in comparison to three-dimensional bulk metal surface plasmonic waves.

(a) Transmission line model for two-dimensional plasmonic medium

As will be discussed shortly, the kinetic energy of the collectively oscillating electrons in a two-dimensional plasmonic wave can be modelled using kinetic inductance of non-magnetic origin [6,9]. On the other hand, the electric potential energy associated with the Coulomb restoring force that drives local electrons into plasmonic oscillation can be modelled using electrical capacitance. Besides the Coulomb restoring force, electron degeneracy pressure serves as another restoring mechanism upon the disturbance of the equilibrium electron density distribution, and this effect can be modelled using quantum capacitance [5,10–12]. This quantum pressure, however, becomes conspicuous only when the Coulomb restoring force is substantially weakened by, for example, placing a gate very proximate to the two-dimensional plasmonic medium and reducing the Coulomb interaction range; throughout this paper, we ignore the quantum effect. Then the two-dimensional plasmonic medium can be modelled as a transmission line consisting of distributed kinetic inductance \( L_k \) per unit length and distributed electrical capacitance \( C \) per unit length (figure 1) [6,9,13]. This plasmonic transmission line differs from the standard electromagnetic transmission line in that the latter employs magnetic inductance instead of kinetic inductance. The plasmonic velocity is then \( v_p = 1/(L_k C)^{1/2} \), which corresponds to the plasmonic dispersion relation.

We first evaluate \( L_k \) in the two-dimensional conductor case where electrons have finite effective mass, \( m^* \), such as in GaAs/AlGaAs 2DEG (width \( W \) and length \( l \)) [9]. Let a time-dependent electric potential \( V(t) \) be applied along the length to induce an electric field \( V(t)/l \). Here, the length \( l \) is chosen so short that the electric field does not exhibit a spatial variation; this is not
Figure 1. Transmission line model of a two-dimensional plasmonic medium. If the medium is gated, the gate serves as the ground. For an un gated medium, the ground is the potential of the free space far enough away. *dx*: infinitesimal segment length of the two-dimensional plasmonic medium.

a limiting assumption, as the goal is to derive the kinetic inductance per unit length. Inertial accelerations occur, for which Newton’s equation of motion for an electron is \(-e(V/l) = m^*(dv/dt)\) (\(v\): electron velocity). This translates to \(-e(V/l) = io\pi m^*v\) in the frequency domain. From this and by noting that the current because of the electrons’ motion is \(I = -n_{2D}evW\) (\(n_{2D}\): electron density per unit area), the two-dimensional conductor’s impedance is obtained: \(V/I = i\omega \times (m^*/n_{2D}\pi^2)(l/W)\). This is inductive impedance of non-magnetic origin, with the kinetic inductance per unit length given by

\[
L_k = \frac{m^*}{n_{2D}\pi^2} \times \frac{1}{W}. \tag{2.1}
\]

By using \(k_F^2 = 2\pi n_{2D}\) and \(E_F = \hbar^2 k_F^2/(2m^*)\) \((k_F\): Fermi wavenumber, \(E_F\): Fermi energy), we can rewrite equation (2.1) as

\[
L_k = \frac{\pi \hbar^2}{e^2} \times \frac{1}{E_F} \times \frac{1}{W}. \tag{2.2}
\]

The kinetic energy of the accelerating electrons is intimately linked to the kinetic inductance. With the velocity \(v\) of an electron at a given time, the total kinetic energy \(K_{\text{total}}\) of the electrons in the two-dimensional conductor strip is expressed \(K_{\text{total}} = m^*v^2/2 \times n_{2D}Wl\). As the total current is \(I = -n_{2D}evW\), we can write

\[
K_{\text{total}} = \frac{1}{2} \times (L_k l) \times I^2, \tag{2.3}
\]

where \(L_k l\) is the total kinetic inductance of the two-dimensional conductor strip. Equation (2.3) is analogous to the energy of a magnetic inductor with current \(I\) given by \(1/2 \times \text{(magnetic inductance)} \times I^2\).

Alternatively, we can instead calculate \(L_k\) by first evaluating the total kinetic energy \(K_{\text{total}}\) and current \(I\) in the \(k\)-space \((k\): electron wavenumber) and then relating them through the energy–current relationship, equation (2.3) [9]. With the electric field applied along the length of the two-dimensional conductor strip to which direction we assign a negative \(x\)-axis, the two-dimensional Fermi disc with diameter \(k_F\) whose centre originally lies at the \(k\)-space origin (figure 2a) shifts towards the positive \(k_x\)-axis, increasing the total kinetic energy and producing a current \(I\). Figure 2b shows the Fermi disc shift by \(\Delta k \ll k_F\), after time \(\Delta t\). The total kinetic energy increase is

\[
K_{\text{total}} =WL \int_B^A 2 \frac{dk_x}{2\pi} \frac{dk_y}{2\pi} E(k) - WL \int_A^B 2 \frac{dk_x}{2\pi} \frac{dk_y}{2\pi} E(k), \tag{2.4}
\]

where the factor 2 in each integrand accounts for spin degeneracy and \(E(k) = \hbar^2 k_F^2/(2m^*)\) is the energy of a single electron whose wavenumber is \(k\). Keeping to the lowest order of \(\Delta k\), it is a straightforward exercise to show that equation (2.4) leads to

\[
K_{\text{total}} = \frac{WIE_F}{2\pi} \times (\Delta k)^2. \tag{2.5}
\]

On the other hand, the current magnitude \(I\) is given by

\[
I = W\int_B^A 2 \frac{dk_x}{2\pi} \frac{dk_y}{2\pi} ev_x(k), \tag{2.6}
\]
Figure 2. Shift of the Fermi disc in the k-space in response to an electric field. (a) Fermi disc and (b) Fermi disc (after acceleration).

where \( v_x(k) \) is the x-component of the velocity of an electron whose wavevector is \( k \), that is, \( v_x(k) = \frac{\hbar k}{m^*} \cos \theta \), where the integration variable \( \theta \) is in reference to figure 2. Keeping to the lowest order of \( \Delta k \), one can show that equation (2.6) reduces to

\[
I = \frac{W e E_F}{\pi \hbar} \times \Delta k.
\] (2.7)

Equations (2.5) and (2.7) satisfy the energy–current relationship of equation (2.3) with \( L_k \) given by

\[
L_k = \frac{\pi \hbar^2}{e^2} \times \frac{1}{E_F} \times \frac{1}{W},
\] (2.8)

which is identical to the \( L_k \)-expression of equation (2.2).

The second approach to calculate \( L_k \) is more general than the first approach, because the second approach can be applied to any arbitrary single electron \( E-k \) dispersion. In particular, in the linear \( E-k \) dispersion case of graphene—another example of two-dimensional conductor—where individual electrons behave as massless particles [14,15], the first approach cannot be used but the calculation in the second approach can be repeated now with \( E(k) = \hbar v_F k \), \( v_x(k) = v_F \cos \theta \), and with the appropriate degeneracy factor including both spin and valley degeneracies (\( v_F \): Fermi velocity) [16]. The application of the second approach to the calculation of the graphene kinetic inductance turns out to be identical to equation (2.8).

The per-unit-length capacitance, \( C \), in the two-dimensional plasmonic transmission line (figure 1), which models the Coulomb restoring force in the plasmonic wave, depends on surroundings of the plasmonic medium. For example, if a two-dimensional conductor strip with width \( W \) has no other conductors nearby, \( C \) for a given plasmonic wavenumber \( k_p \) is given by [17,18]

\[
C = 2 \varepsilon k_p W,
\] (2.9)

where \( \varepsilon \) is the electric permittivity of the surroundings. This is obtained by calculating the electric energy of the sinusoidal charge density distribution at a plasmonic wavenumber, \( k_p \).

As the plasmonic velocity is \( v_p = \omega/k_p = 1/(L_k C)^{1/2} \), we can now obtain the detailed expression for the two-dimensional plasmonic dispersion. In the case of the stand-alone two-dimensional conductor where \( C \) is given by equation (2.9), by using \( L_k \) of equation (2.8), whether the two-dimensional conductor is semiconductor 2DEG or graphene, we obtain

\[
\omega = \frac{k_p}{\sqrt{L_k C}} = \sqrt{\frac{e^2 E_F}{2 e \pi \hbar^2}} k_p.
\] (2.10)

Calculation in the random phase approximation framework yields a more general form of the two-dimensional plasmonic dispersion relation [5,19], but in the limit where quantum effects such as electron degeneracy pressure and interband transitions can be ignored, the general dispersion reduces to equation (2.10) for both semiconductor 2DEG and graphene [5,20].
If an external conductor is proximate to the two-dimensional conductor, C is altered. A case of particular interest is a gated two-dimensional conductor. If the separation, d, between the gate and two-dimensional conductor is much smaller than the plasmonic wavelength ($k_p d \ll 1$), C becomes the parallel plate capacitance per unit length, $C = \varepsilon W/d$. The two-dimensional plasmonic dispersion then becomes linear for both semiconductor 2DEG and graphene [11, 21]

$$\omega = \frac{k_p}{\sqrt{L_k C}} = k_p \sqrt{\frac{e^2 E_F d}{\varepsilon \pi \hbar^2}}. \quad (2.11)$$

When compared with the stand-alone two-dimensional conductor, the gated configuration yields smaller plasmonic wavelength and velocity (equations (2.10) versus (2.11)). This is because the gate shortens the Coulomb interaction range. For the same reason, as d is shortened, the plasmonic velocity and wavelength are further reduced. These two-dimensional plasmonic dispersions for stand-alone or gated cases have been experimentally demonstrated for both semiconductor 2DEG [6, 8] and more recently for graphene [7, 22, 23].

**(b) Two-dimensional plasmons versus three-dimensional surface plasmons**

Although we have focused on the transmission line model for the two-dimensional plasmonic medium, a similar transmission line model consisting of kinetic inductance and electrical capacitance can be used to model the surface plasmonic medium in the skin of the three-dimensional bulk metal with the finite penetration depth, for the two main energetic components of the surface plasmonic wave on the three-dimensional metal are also the kinetic energy of collectively oscillating electrons and the electric potential energy corresponding to the Coulomb restoring force [18]. By contrast, light waves possess magnetic and electric energies as two energetic components. By comparison, one can see that the kinetic energy of plasmonic waves (whether two-dimensional plasmons or three-dimensional surface plasmons) is responsible for their behavioural divergence from light waves.

To describe the behavioural difference between two-dimensional plasmonic waves and three-dimensional metal surface plasmonic waves, we now evaluate the kinetic inductance associated with the three-dimensional surface plasmonic wave. The collective oscillation of electrons in three-dimensional surface plasmonic waves occurs within the skin of a bulk conductor, whose frequency-dependent penetration depth, $\delta$, decreases with increasing frequency. The per-unit-length kinetic inductance of this skin with width $W$ can be derived by considering inertial acceleration of electrons therein, as in the first approach given in § 2b (for three-dimensional conductors, there is no particular reason to consider massless electrons)

$$L_{k, \text{skin}} = \frac{m^*}{n_{3D} \varepsilon^2} \times \frac{1}{W \delta}, \quad (2.12)$$

where $n_{3D}$ is conduction electron density per unit volume. Using $k_F^3 = 3\pi^2 n_{3D}$ and $E_F = \hbar^2 k_F^2/(2m^*)$, we can rewrite equation (2.12) into

$$L_{k, \text{skin}} = \frac{3\pi^2 \hbar^2}{2e^2} \times \frac{1}{E_F} \times \frac{1}{W} \times \frac{1}{k_F \delta}. \quad (2.13)$$

Equations (2.13) and (2.8) show that kinetic inductance in either three- or two-dimensional case increases as the total number of electrons is reduced. This can be understood as follows. When there are fewer electrons, they need to accelerate to a proportionally higher velocity to produce the same current. The total kinetic energy then becomes larger, as it is proportional to the number of electrons but to the square of the electron velocity. As we have fixed the current, the kinetic inductance then should be larger, according to equation (2.3).

When two-dimensional kinetic inductance $L_k$ of equation (2.8) and three-dimensional kinetic inductance $L_{k, \text{skin}}$ of equation (2.13) are juxtaposed, the $1/(k_F \delta)$ factor in $L_{k, \text{skin}}$ makes an apparent difference. As the penetration depth $\delta$ decreases with frequency in the three-dimensional surface plasmonic dynamics, $L_{k, \text{skin}}$ increases with frequency; this is essentially because the reduced $\delta$
decreases the number of conduction electrons participating in the surface plasmonic wave. At frequencies below the optics regime, $\delta$ is large enough to render $L_{k,\text{skin}}$ unappreciable when compared with the magnetic inductance of the surface plasmonic medium. Hence, it is difficult to observe surface plasmons below the optics regime with three-dimensional metals, and three-dimensional surface plasmonic dispersion curve deviates away from the light dispersion line only towards the optics regime (figure 3). By contrast, $L_k$ of the two-dimensional plasmonic medium has no frequency dependency, as there is no such frequency-dependent penetration depth where electrons are confined perfectly into two dimensions. Moreover, $L_k$ is orders of magnitude larger than the magnetic inductance of the two-dimensional conductor. Therefore, the two-dimensional plasmonic wave emerges far below the optics regime, with its dispersion curve deviating significantly away from the light line at these low frequencies (figure 3).

Even when $L_{k,\text{skin}}$ becomes appreciable in the optics regime with small enough $\delta$ and surface plasmonic dynamics is more pronounced, $k_F\delta$ is still much larger than 1, leaving $L_{k,\text{skin}} \ll L_k$ (in principle $L_{k,\text{skin}}$ can grow indefinitely as frequency grows towards the surface plasmon resonance frequency with $\delta$ approaching 0, but in practice loss obscures such excitations). The $L_{k,\text{skin}} \ll L_k$ inequality is further enhanced by the fact that $E_F$ appearing in both $L_{k,\text{skin}}$ and $L_k$ is typically much larger with the three-dimensional bulk metal such as gold than with semiconductor 2DEG and graphene. Overall, $L_{k,\text{skin}}$ even in the optics regime is far smaller than $L_k$ by two to three orders of magnitude. As $v_p \propto [\text{kinetic inductance}]^{-1/2}$, two-dimensional plasmonic velocity is far smaller than three-dimensional surface plasmonic velocity typically limited to approximately $c/10$ [1] (figure 3), achieving far greater ultra-subwavelength confinement. One can further slow the two-dimensional plasmonic wave by placing a gate proximate to the two-dimensional conductor and thus by shortening the Coulomb interaction range within the two-dimensional conductor (i.e. by increasing $C$; note that $v_p = 1/(L_k C)^{1/2}$) (equation (2.10) versus equation (2.11); figure 3); in fact, with top-gated GaAs 2DEG, we were able to obtain two-dimensional plasmonic velocities as low as approximately $c/700$ [6].

(c) Effect of electron scattering

Electron scatterings with phonons and lattice impurities in the two-dimensional plasmonic medium are manifested as per-unit-length ohmic resistance $R$, which can be added to the transmission line model of figure 1 in series with $L_k$. The quality factor of the two-dimensional
plasmonic medium is then given by

\[ Q = \frac{wLk}{R} = \frac{w}{\tau}, \]

where the electron scattering time \( \tau \) factors in through \( R \) (note that we here are not considering loss mechanisms owing to interband transitions, for in practice many plasmonic applications can be considered at frequencies where such transitions do not occur). The plasmonic dynamics can be observed as far as \( Q \) is not too far below 1, i.e. if \( \tau \) is long enough to accommodate an appreciable kinetic energy increase (if \( Q \) is much larger than 1, many cycles of collective electron oscillation are sustained between scattering events, making the plasmonic wave very easily observable). To observe two-dimensional plasmonic waves at gigahertz frequencies, \( \tau \) has to be increased, which can be done by cryogenic operation, as applicable for GaAs/AlGaAs 2DEG where \( \tau \) is limited by phonon scattering down to substantially lowered temperature, but not as well with graphene where impurity scattering is significant even at room temperature. At terahertz and infrared frequencies, room temperature plasmonic operation is possible with both semiconductor 2DEG and graphene, as experimentally demonstrated [7,24].

3. Applications: ultra-subwavelength two-dimensional plasmonic circuits and metamaterials

A two-dimensional plasmonic medium can be readily shaped into a designer planar geometry by using the standard fabrication technology. Two-dimensional plasmonic waves then can be manipulated by reflections, interferences and superposition according to the geometry. In this way, one can create a variety of gigahertz to terahertz and infrared two-dimensional plasmonic circuits and metamaterials [6,8,9]. Owing to their ultra-subwavelength confinement, these two-dimensional plasmonic functional structures are amenable to near-field operation, sub-diffraction-limit imaging, and drastic miniaturization.

An example of two-dimensional plasmonic circuits is plasmonic bandgap crystals, which can be created by introducing structural periodicity into a two-dimensional conductor. These plasmonic bandgap crystals are analogous to photonic bandgap crystals [25,26], but the former operate far below the optical frequencies and exhibit much greater subwavelength confinement. A proof-of-concept two-dimensional plasmonic crystal, which Andress et al. [6] built from GaAs/AlGaAs 2DEG and operates in the gigahertz frequencies at cryogenic temperature (4.2 K), is shown in figure 4. The 2DEG was periodically shaped by spatially modulating its width (figure 4a) and was placed between electromagnetic metallic coplanar waveguides (CPWs), consisting of signal (S) and ground (G) lines, where the S lines couple to the 2DEG via ohmic contacts (figure 4a,b). The 2DEG is placed under a metallic gate, which is merged with the CPWs’ G lines; in this way, the top gate not only enhances the subwavelength confinement of two-dimensional plasmonic waves, but serves as the proper plasmonic ground. Owing to the crystal periodicity, the magnitude of the transmission parameter \( s_{21} \) obtained from microwave scattering measurements shows a bandgap (24–34 GHz) around the first Brillouin-zone boundary (figure 4c), where the crystal periodicity equals half the plasmonic wavelength, indicating \( v_p \sim c/300 \). The phase of the measured \( s_{21} \) is a product of plasmonic wavenumber \( k_p \) and the crystal length, thus, \( s_{21} \)’s phase over the frequency (figure 4d) yields the dispersion, which also shows the bandgap behaviour. Its passband slope, which is linear owing to the gating (equation (2.11)), consistently indicates \( v_p \sim c/300 \).

The shaping principle can be applied with a wealth of versatility. For instance, one can subtly vary the crystal shape to introduce an appreciable behavioural difference. Figure 5a shows an example variation [6], where the transitions between narrow and wide 2DEG sections are abrupt. Plasmonic dynamics here is not a merely disturbed horizontal routing as in figure 4. Vertical routing of plasmons to and from the ends of the thick sections (stubs) must be considered; in fact, these stubs serve as plasmonic cavities that resonate by forming a \( \lambda_p/4 \) standing wave (or its harmonics at higher frequencies), a superposition of plasmonic waves travelling to and
reflected from the stub ends. Thus, the repetition of the stubs results in an extra bandgap (approx. 52 GHz) arising from the $\lambda_p/4$ standing wave resonance, in addition to the Brillouin-zone-boundary bandgap (figure 5b,c). By further exploiting the versatility of two-dimensional medium shaping, Andress et al. also created plasmonic crystals with two-directional periodicity by
etching periodic lattices of holes into 2DEG (figure 6a). For two-dimensional plasmons travelling horizontally, a bandgap occurs around the first Brillouin-zone boundary, at which the separation between two adjacent vertical crystal planes equals \( \lambda_p/2 \). Indeed, two rectangular lattices and a hexagonal lattice made out of 2DEG in figure 6a produce expected bandgaps measurements (figure 6b).

Another exciting avenue to explore is to create plasmonic interferometers. We recently demonstrated a two-path interferometer of Mach–Zehnder type where two two-dimensional
plasmonic waves undergoing different phase delays are made to interfere [8]. These on-chip two-dimensional plasmonic interferometers exhibit a higher sensitivity to the effective path length difference when compared with interferometers employing electromagnetic waves, owing to two-dimensional plasmons’ ultra-subwavelength confinement. The two-dimensional plasmonic interferometers may thus be useful for highly precise and sensitive signal detection, modulation and demodulation, and biomolecular and chemical sensing, in particular, at terahertz and infrared frequencies.

Negative index metamaterials have been a topic of interest owing to their unusual abilities that can lead to technologically gainful applications, and a broad array of negative index metamaterials has been synthesized by engineering electric, magnetic or optical properties of materials [27–31]. Ultra-subwavelength two-dimensional plasmons, in particular their associated large two-dimensional kinetic inductance, can be engineered by shaping the two-dimensional conductor geometry to create a new type of metamaterials with extraordinarily strong negative refraction. Using kinetic inductance for negative refraction was envisioned with three-dimensional metallic nanoparticles [32] and experimentally glimpsed with three-dimensional metal surface plasmons [33], but three-dimensional kinetic inductance is far smaller than two-dimensional kinetic inductance, and the two works yielded negative indices less than −5. By contrast, we recently obtained a negative index as large as −700 by exploiting the large two-dimensional kinetic inductance [9]. The large negative index, which corresponds to ultra-subwavelength confinement of a negatively refracting wave, can bring the science of negative refraction into drastically miniaturized scale and enable sub-diffraction-limit imaging.

Figure 7 shows a proof-of-concept negative index metamaterial operating at gigahertz frequencies and cryogenic temperature (up to 20 K) from the aforementioned work of ours [9]. It is an array of ungated GaAs/AlGaAs 2DEG strips (figure 7a,b). Metallic CPWs consisting of signal lines (S) flanked by ground lines (G) are used to guide signals to and from the device. Each 2DEG strip is tied to the G lines at its both ends via ohmic contacts. The left S line extends up to over a few strips on the left-hand side. The excitation electromagnetic wave’s electric fields between the signal and ground lines of the left CPW excites two-dimensional plasmonic waves in the leftmost few strips along the direction of the strips. The resulting modulation of charge distribution in these strips capacitively couple to the neighbouring strip to the right, exciting two-dimensional plasmonic waves along the direction of the strip. This energy transfer process is repeated, delivering an effective wave from left to right, perpendicularly to 2DEG strips. Note that two types of waves are involved (figure 7c); the two-dimensional plasmonic wave travelling along each strip, and the effective wave propagating orthogonally to the strips. It is this effective wave that is negatively refracting.

As no current passes across any strip centre owing to symmetry, only the lower half below the horizontal symmetry line, or half circuit, can be used in understanding the metamaterial. If we denote the voltage at the top end of the $n$th half strip as $V_m(t)$, the effective wave can be represented by \{ $V_1(t), V_2(t), V_3(t), \ldots$ \} (figure 7c). Each half strip may be modelled as a plasmonic transmission line supporting a two-dimensional plasmonic wave (figure 7c). But as the plasmonic transmission line is short-circuit terminated to ground at its end and the plasmonic wavelength is much longer than the strip length in this design, the plasmonic transmission acts like a lumped two-dimensional kinetic inductor, $L_{kl}$, where $l$ is the effective length of the half strip. The entire half-circuit is then an array of capacitively coupled lumped kinetic inductors (figure 7d). This may be likened to the left-handed electromagnetic transmission line, an array of capacitively coupled magnetic inductors, which is known to be negatively refracting [34,35]. However, with the significantly large two-dimensional kinetic inductance, the 2DEG strip array yields a negative index as large as $−700$ [9], while the left-handed electromagnetic transmission line, which relies on three to four orders of magnitude smaller magnetic inductance, yields negative indices typically below $−5$.

We reviewed the unique characteristics of two-dimensional plasmonic waves (in particular, their ultra-subwavelength confinement) and their underlying physics and described how two-dimensional plasmonic waves can be engineered by geometric shaping of two-dimensional
Figure 7. (a) 2DEG strip array. (b) Schematic with the front face cut at the dashed line of part (a). (c) Half-circuit model for the metamaterial. (d) The half 2DEG strip in part (c), which is a two-dimensional plasmonic medium, may be modelled as a lumped kinetic inductor, if the plasmonic wavelength is much longer than the half 2DEG strip. Reprinted with permission from [9]. Copyright 2012 Nature Publishing Group. (Online version in colour.)

conductor to create two-dimensional plasmonic circuits and metamaterials. The proof-of-concept devices presented were implemented with GaAs 2DEG, and operated at gigahertz frequencies, thus at cryogenic temperature. However, room temperature excitation of two-dimensional plasmonic waves is possible at terahertz and infrared frequencies with both GaAs 2DEG and graphene [7,24], thus the demonstrated device designs can be scaled to these higher frequencies for room temperature operation.

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